

(* This is an example of a world magnetic map using coefficients from NOAA. The particular coefficients used here are from an older list of coefficients. Updates can be found at http://www.ngdc.noaa.gov/geomag/WMM/data/WMM2010/WMM2010_Report.pdf or https://www.ngdc.noaa.gov/geomag/WMM/data/WMM2010/WMM2010_Report.pdf The representation in the map shown below is for the Total Field and all the expressions for other representations (i.e., declination, etc) are given . *)

$$\text{legendrep}[n_ , m_ , x_] := \text{Which}[m == 0, 1, m > 0, \sqrt{2}] * \sqrt{\frac{(n-m)!}{(n+m)!}} * \text{LegendreP}[n, m, x]$$

$$v = a \text{ Sum} \left[\left(\frac{a}{r} \right)^{n+1} \left(\frac{g}{n} \text{Cos}[m \lambda_e] + \frac{h}{n} \text{Sin}[m \lambda_e] \right) \text{legendrep}[n, m, \text{Cos}[\phi]], \{n, 1, 10\}, \{m, 0, n\} \right];$$

$$\text{north} = \frac{1}{r} D[v, \phi];$$

$$\text{east} = \frac{-1}{r \text{Sin}[\phi]} D[v, \lambda_e];$$

$$\text{down} = D[v, r];$$

$$\text{horizontal} = \sqrt{\text{north}^2 + \text{east}^2};$$

$$\text{total} = \sqrt{(\text{north}^2 + \text{east}^2 + \text{down}^2)};$$

$$\text{graddown} = D[\text{total}, r];$$

$$\text{declination} = \frac{180}{\text{Pi}} \text{ArcTan}[\text{north}, \text{east}];$$

$$\text{inclination} = \frac{180}{\text{Pi}} \text{ArcTan}[\text{horizontal}, \text{down}];$$

$$a = 6371.2 \times 10^3;$$

$$g_1^0 = -2.9775 \times 10^4; g_1^1 = -1851;$$

$$g_2^0 = -2136; g_2^1 = 3058; g_2^2 = 1639;$$

$$g_3^0 = 1315; g_3^1 = -2240; g_3^2 = 1246; g_3^3 = 807;$$

$$g_4^0 = 939; g_4^1 = 782; g_4^2 = 324; g_4^3 = -423; g_4^4 = 142;$$

$$g_5^0 = -211; g_5^1 = 353; g_5^2 = 244; g_5^3 = -111; g_5^4 = -166; g_5^5 = -37;$$

$$g_6^0 = 61; g_6^1 = 64; g_6^2 = 60; g_6^3 = -178; g_6^4 = 2; g_6^5 = 17; g_6^6 = -96;$$

$$g_7^0 = 77; g_7^1 = -64; g_7^2 = 4; g_7^3 = 28; g_7^4 = 1; g_7^5 = 6; g_7^6 = 10; g_7^7 = 0;$$

$$g_8^0 = 22; g_8^1 = 5; g_8^2 = -1; g_8^3 = -11; g_8^4 = -12; g_8^5 = 4; g_8^6 = 4; g_8^7 = 3; g_8^8 = -6;$$

$$g_9^0 = 4; g_9^1 = 10; g_9^2 = 1; g_9^3 = -12; g_9^4 = 9; g_9^5 = -4; g_9^6 = -1; g_9^7 = 7; g_9^8 = 2; g_9^9 = -6;$$

$$g_{10}^0 = -4; g_{10}^1 = -4; g_{10}^2 = 2; g_{10}^3 = -5; g_{10}^4 = -2; g_{10}^5 = 4; g_{10}^6 = 3; g_{10}^7 = 1; g_{10}^8 = 2; g_{10}^9 = 3; g_{10}^{10} = 0;$$

$$h_1^0 = 0; h_1^1 = 5411;$$

$$h_2^0 = 0; h_2^1 = -2278; h_2^2 = -380;$$

$$h_3^0 = 0; h_3^1 = -287; h_3^2 = 293; h_3^3 = -348;$$

$$h_4^0 = 0; h_4^1 = 248; h_4^2 = -240; h_4^3 = 87; h_4^4 = -299;$$

$$h_5^0 = 0; h_5^1 = 47; h_5^2 = 153; h_5^3 = -154; h_5^4 = -69; h_5^5 = 98;$$

$$h_6^0 = 0; h_6^1 = -16; h_6^2 = 83; h_6^3 = 68; h_6^4 = -52; h_6^5 = 2; h_6^6 = 27;$$

$$h_7^0 = 0; h_7^1 = -81; h_7^2 = -27; h_7^3 = 1; h_7^4 = 20; h_7^5 = 16; h_7^6 = -23; h_7^7 = -5;$$

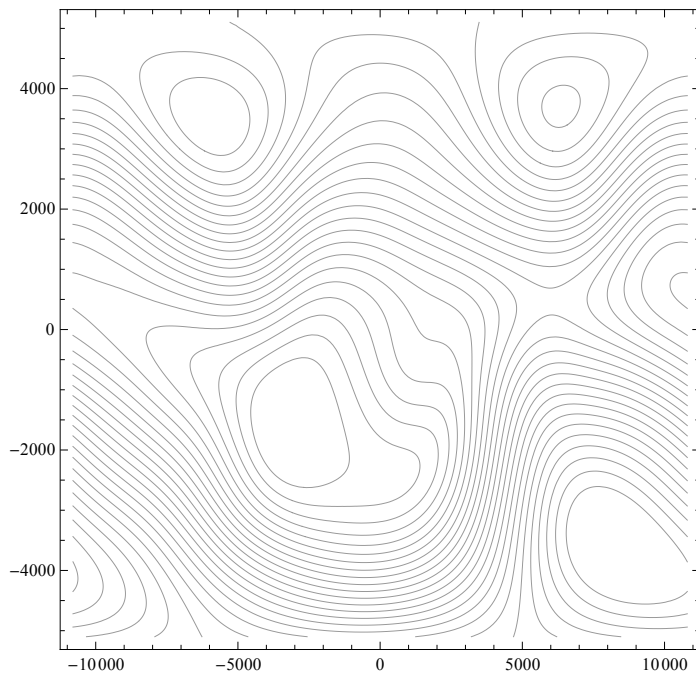
$$h_8^0 = 0; h_8^1 = 10; h_8^2 = -20; h_8^3 = 7; h_8^4 = -22; h_8^5 = 12; h_8^6 = 11; h_8^7 = -16; h_8^8 = -11;$$

$$h_9^0 = 0; h_9^1 = -21; h_9^2 = 15; h_9^3 = 10; h_9^4 = -6; h_9^5 = -6; h_9^6 = 9; h_9^7 = 9; h_9^8 = -7; h_9^9 = 2;$$

$$h_{10}^0 = 0; h_{10}^1 = 1; h_{10}^2 = 0; h_{10}^3 = 3; h_{10}^4 = 6; h_{10}^5 = -4; h_{10}^6 = 0; h_{10}^7 = -1; h_{10}^8 = 4; h_{10}^9 = 0; h_{10}^{10} = -6;$$

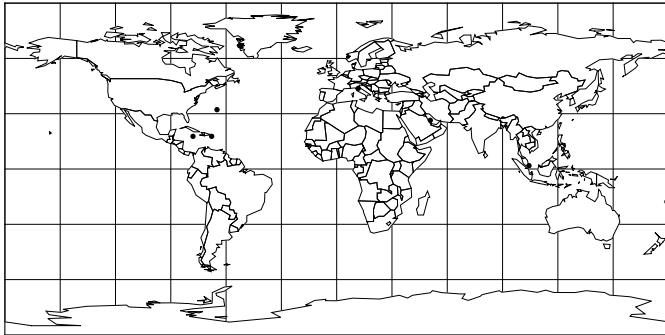
$$r = a + 1000; \phi = -\left(90 + \frac{\text{latitude}}{60}\right) \frac{\text{Pi}}{180} + \text{Pi}; \lambda_e = \frac{\text{longitude}}{60} \frac{\text{Pi}}{180} + \text{Pi};$$

```
tfcon = ContourPlot[total, {longitude, -180 * 60, 180 * 60},  
  {latitude, -85 * 60, 85 * 60}, Contours → 25, PlotPoints → 50, ContourShading → None]
```

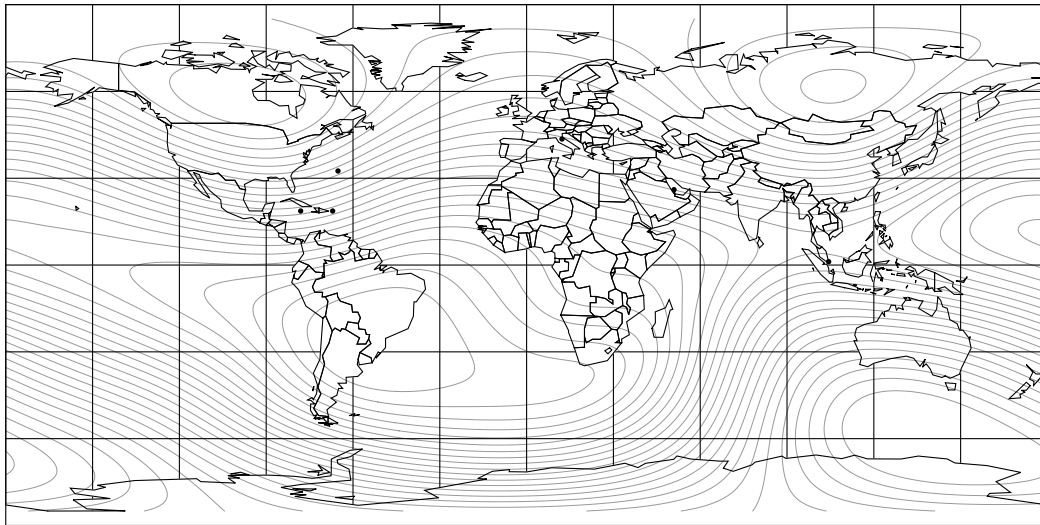


```
<< WorldPlot`
```

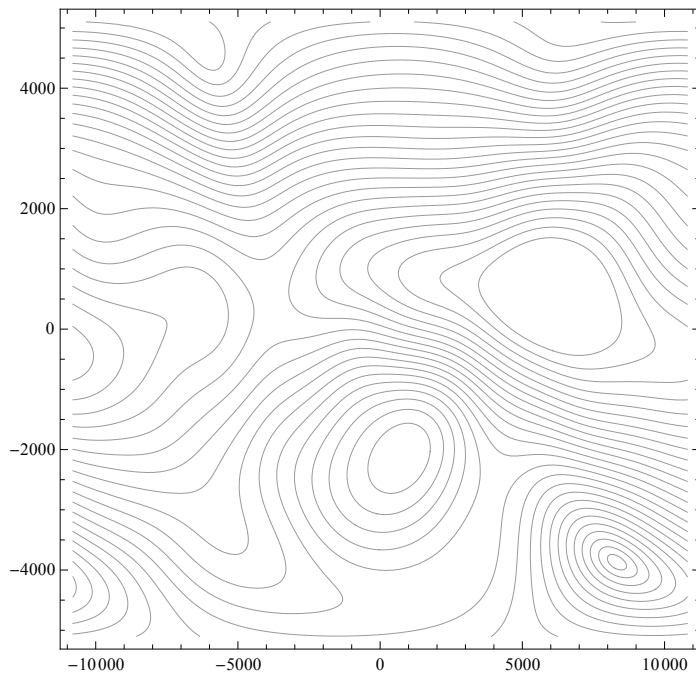
```
world = Graphics[WorldPlot[World]]
```



Show[world, tfcon] (* Total Field Contour Plot on World Map*)

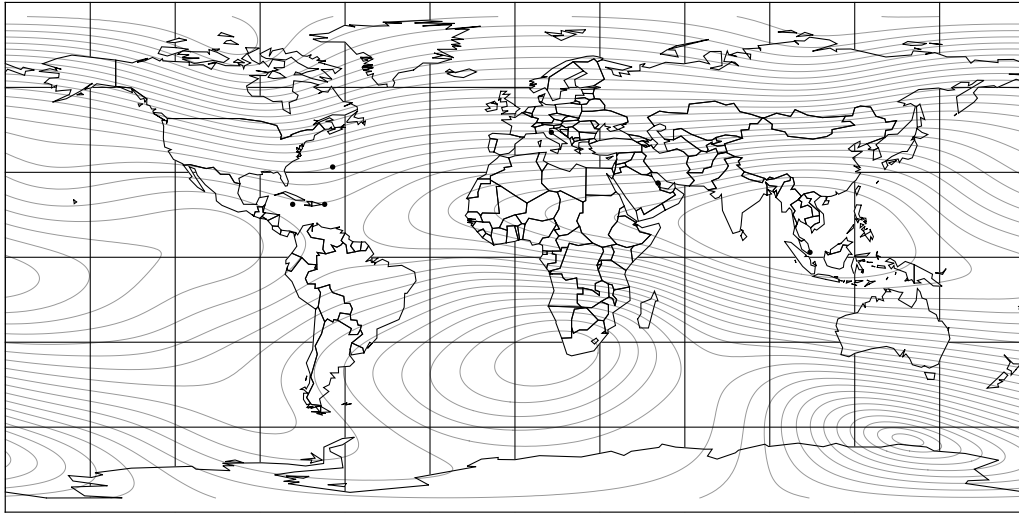


```
horizontalcon = ContourPlot[horizontal, {longitude, -180 * 60, 180 * 60},  
  {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```

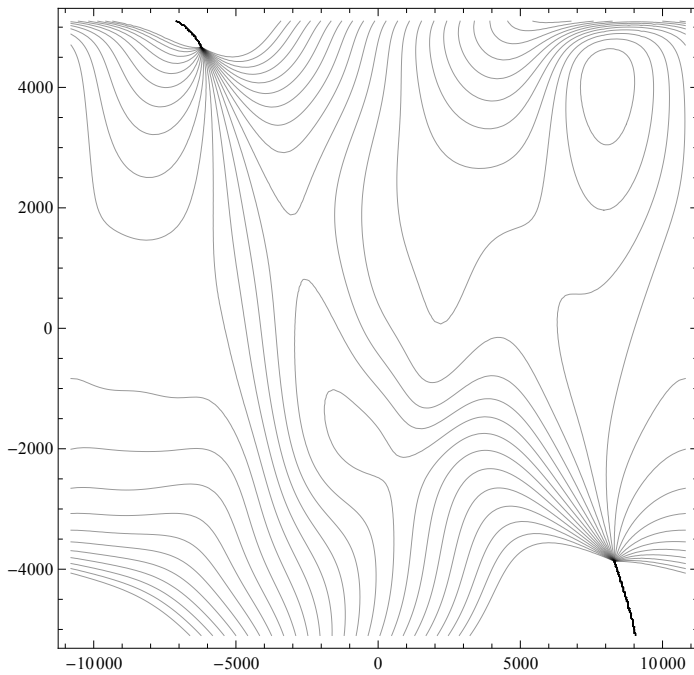


Show[world, horizontalcon]

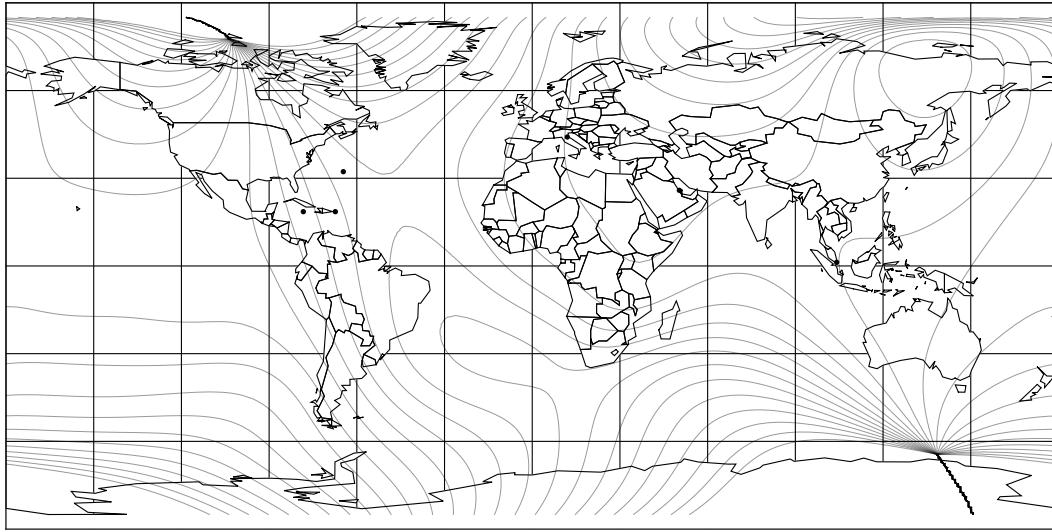
(* Horizontal Component of Total Field Countour Plot on World Map*)



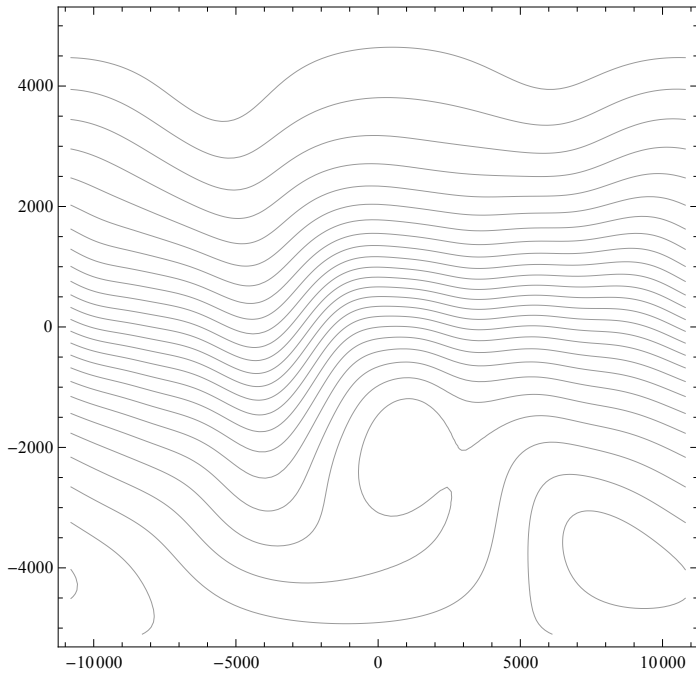
```
declinationcon = ContourPlot[declination, {longitude, -180 * 60, 180 * 60},
    {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```



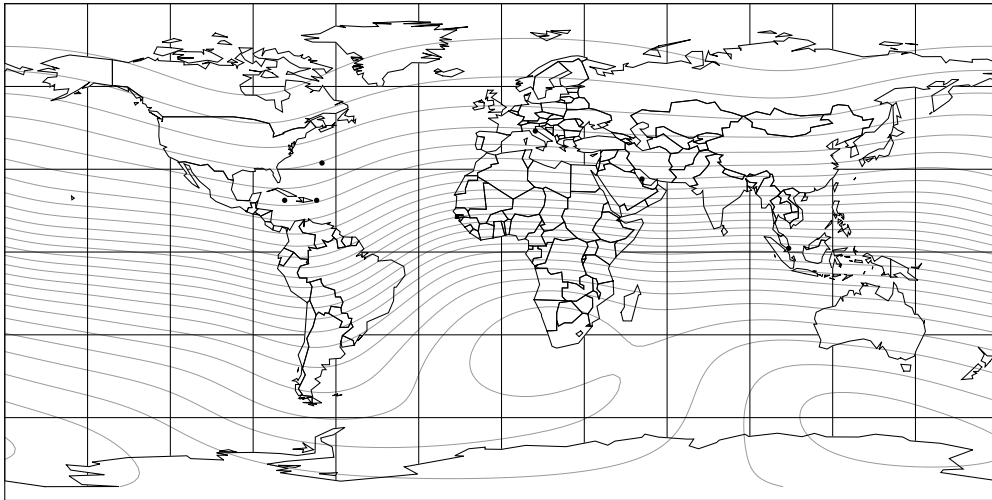
```
Show[world, declinationcon] (* Declination Countour Plot on World Map*)
```



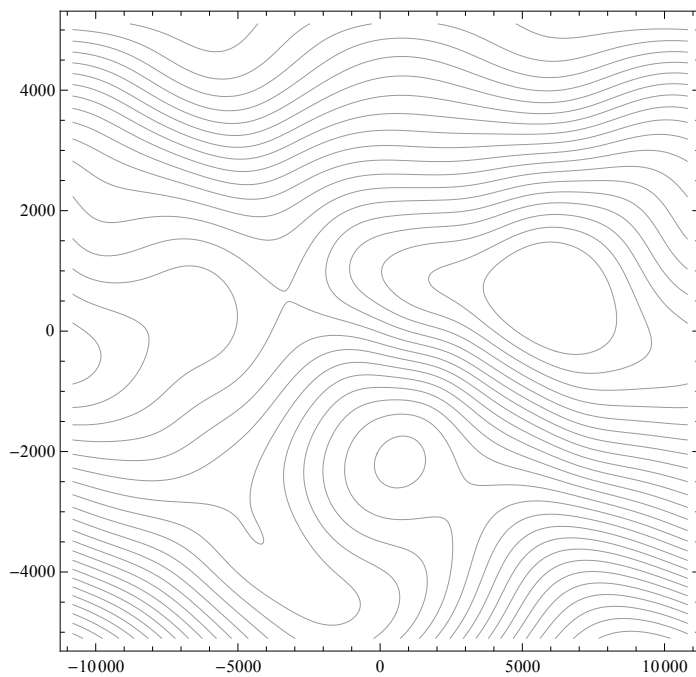
```
inclinationcon = ContourPlot[inclination, {longitude, -180 * 60, 180 * 60},  
  {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```



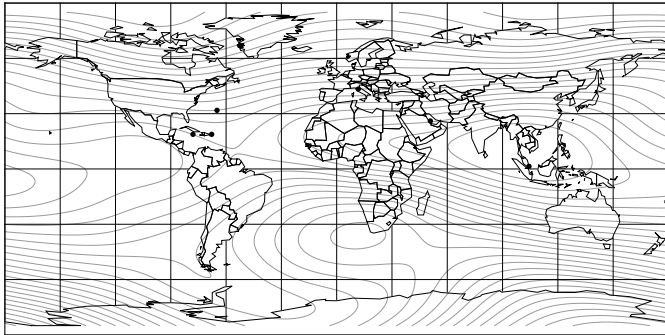
Show[world, inclinationcon] (* Inclination Countour Plot on World Map*)



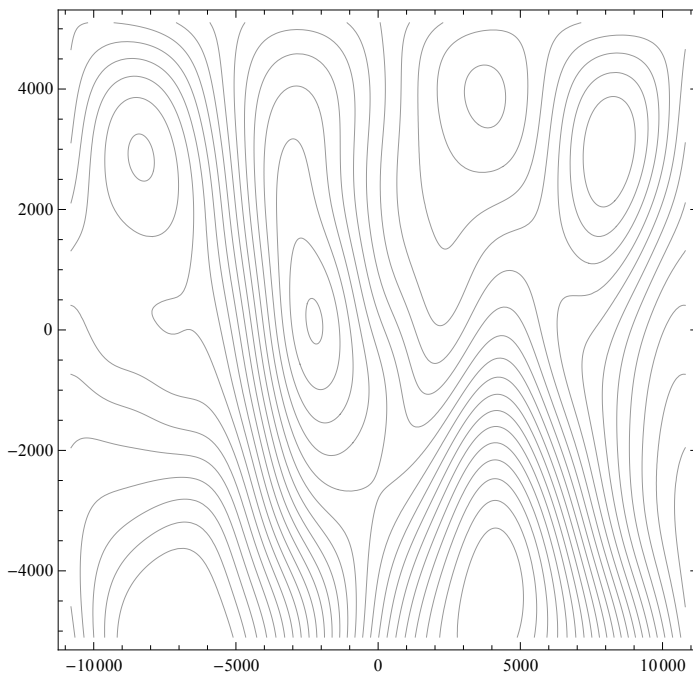
```
northcon = ContourPlot[north, {longitude, -180 * 60, 180 * 60},
  {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```



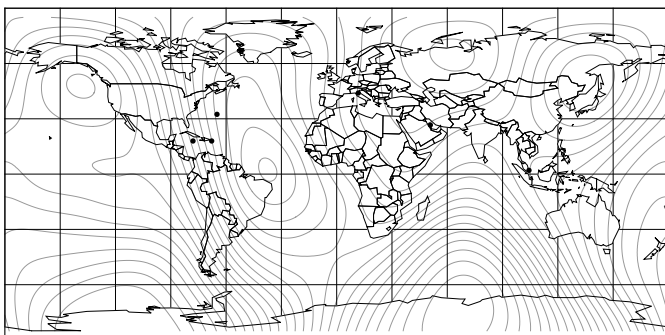
Show[world, northcon] (* North Component Countour Plot on World Map*)



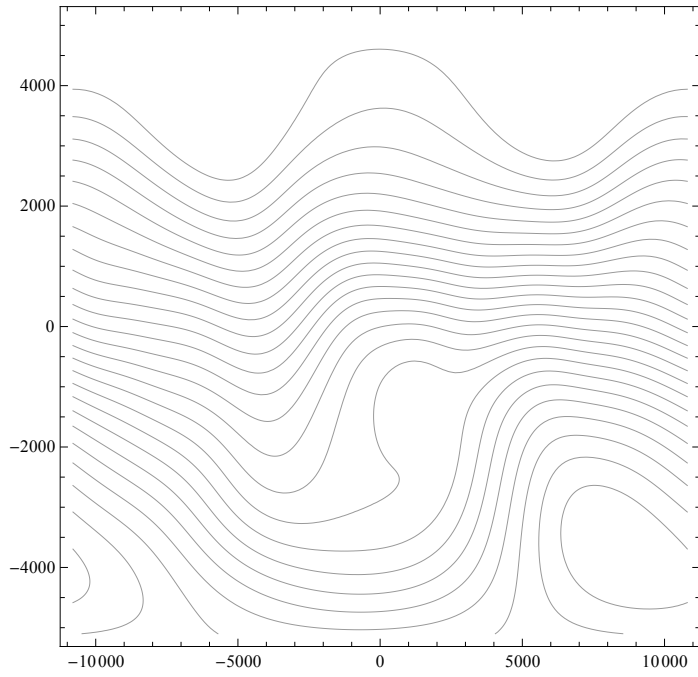
```
eastcon = ContourPlot[east, {longitude, -180 * 60, 180 * 60},  
  {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```



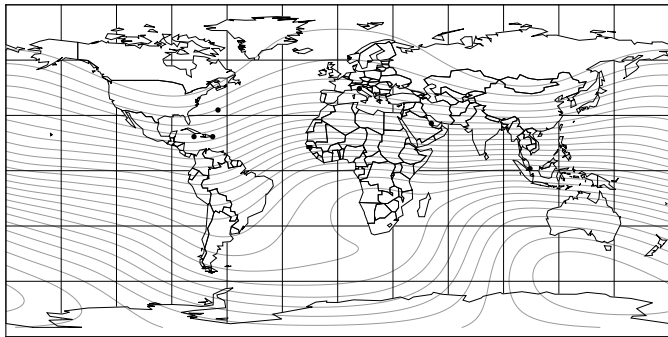
Show[world, eastcon] (* East Component Countour Plot on World Map*)



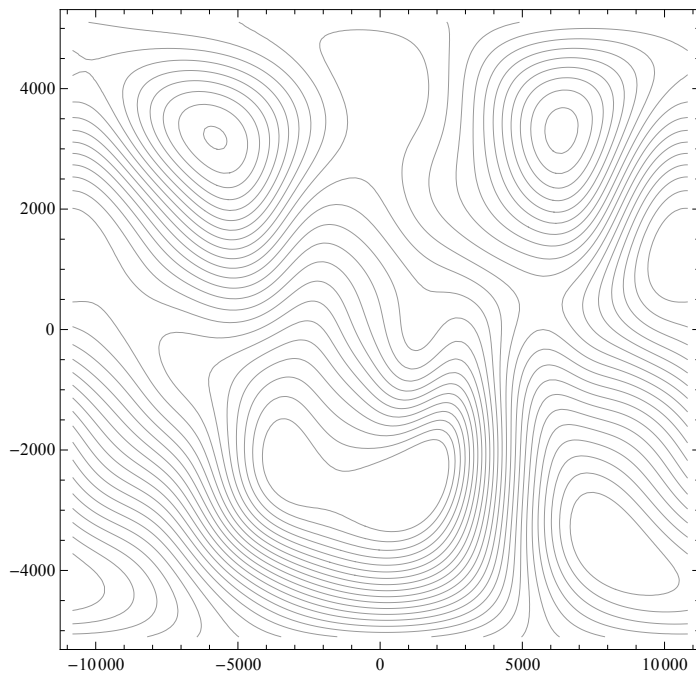
```
downcon = ContourPlot[down, {longitude, -180 * 60, 180 * 60},
  {latitude, -85 * 60, 85 * 60}, Contours -> 25, PlotPoints -> 50, ContourShading -> None]
```



```
Show[world, downcon] (* Down Component Countour Plot on World Map*)
```



```
graddowncon = ContourPlot[graddown, {longitude, -180 * 60, 180 * 60},  
  {latitude, -85 * 60, 85 * 60}, Contours → 25, PlotPoints → 50, ContourShading → None]
```



```
Show[world, graddowncon]
```

(* Gradient Downward Component of Total Field Countour Plot on World Map*)

